

Lossy Trapdoor function の幾つかの亜種について

On some variants of lossy trapdoor function

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あらまし

$\lambda \in \mathbb{N}$ をセキュリティパラメータとすると lossy trapdoor function とは次の確率的多項式時間アルゴリズムの組 $(\text{Gen}, \text{Eval}, \text{Invert})$ である。

$\text{Gen} : 1^\lambda, b \xrightarrow{\$} (s, t)$ where $t = \perp$ if $b = 1$.

$\text{Eval} : s, x \xrightarrow{\$} f_s(x)$ where
 f_s is injective if $b = 0$, and lossy if $b = 1$.

$\text{Invert} : t, f_s(x) \xrightarrow{\$} x$ if $b = 0$.

ここで、関数 f_s の定義域を X とすると、 $b = 0$ のとき $|f_s(X)|/|X| = 1$ (即ち単射) $b = 1$ のとき $|f_s(X)|/|X| \sim O(2^{-\lambda})$ であつ $\{s|(s, t) \leftarrow \text{Gen}(1^\lambda, 0)\}$ の分布と $\{s|(s, t) \leftarrow \text{Gen}(1^\lambda, 1)\}$ の分布が λ に関して計算量的に識別不能とする。Peikert と Waters は STOC 2008 において lossy trapdoor function の概念を提唱し、その具体的構成と応用を提案した [1–3]。その後 lossy trapdoor function の構成法や拡張および応用などに関して様々な研究が行われている [4–8]。本発表では Lossy Trapdoor function の幾つかの亜種について考察を行う。

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